Numerical study of built-in cylinders’ effects on flow pattern and heat transfer characteristics in a laminar channel flow

Sajad Rezazadeh*, Mohammadreza Mataji Amirrud, Mohammad Raad* and Davoud Abbasinezhad Fallah*

*Faculty of Mechanical Engineering, Urmia University of Technology, Urmia, Iran.
Faculty of Energy and Environment Department, School of Environment, College of Engineering, University of Tehran, Tehran, Iran.

Abstract
A numerical simulation of laminar fluid flow and heat transfer over built-in cylinders in a channel is presented. Effects of cylinders that located in a rectangular channel with constant wall temperature on flow and heat transfer have been investigated by the drag coefficient on cylinders wall, skin-friction factor on channel wall, Strouhal number, pumping factor, Nusselt number, and Performance Index (PI) factor, which denote the heat transfer in terms of the pressure drop. Results are validated by the most reliable published works in the literature. Effects of Reynolds number and blockage ratio ($\beta$) for the equilateral triangular cylinder for $120 \leq \text{Re} \leq 180$ and $0.15 \leq \beta \leq 0.55$ on flow and heat transfer are investigated with more details. Results indicated that by increasing $\text{Re}$ for constant blockage ratio, the drag coefficient, skin-friction coefficient, pumping factor, and Strouhal number increase; but the Nusselt number diminishes and PI factor has an optimum range. Furthermore, results reveal that variation in blockage ratio has more significant effects on the flow and heat transfer than variation in Reynolds number.

1. Introduction
The classical problem of flow over bluff bodies is a major interest in the fluid mechanics, due to its relevancy to engineering applications, e.g. suspension of bridges, automobile manufacturing, aerospace, chemical engineering, cooling of the electronic components, etc. [1-6]. Also, more recently, with increasing demand in energy consumption, this problem gains additional interest in the field of magnetohydrodynamic electricity production [7-9]. Pertinently, this problem has been one of the major topics for investigation by numerous scientists [10]. In 1969, Johnson and Joubert [11] experimentally studied the effects...
of vortex generators (VG) on airstream by using a cylinder which was fitted with two rows of VGs. Their results show both a decrease in drag coefficient and an increase in Nusselt number that can be obtained when VGs are fitted. Noack and Eckelmann [12] practiced Galerkin method to investigate flow over a circular cylinder. They obtained the beginning of the laminar vortex shedding at $Re_{crit}=53.3$ and this regime lasts until $Re=170$ which induces three-dimensional calculations due to 3-D instabilities of flow. Zdravkovich [13] presented a classification of flow over circular cylinder and ascribed periodic laminar wake to $30<Re<150$. Williamson [14] conducted a comprehensive classification of this problem by means of the base suction coefficient and showed that the laminar vortex shedding regime happens at $49<Re<140$. Suzuki et al. [15] investigated the numerical solution for unsteady laminar flow over a square rod placed at the channel center. They considered variation of the blockage ratio and Reynolds number, and they found that the blockage ratio is a major factor in appearance of the periodic motion of the flow. The numerical investigation of flow and heat transfer characteristics of a heated square cylinder in laminar channel flow was carried out by Sharma and Eswaran [16]. They observed increase in Strouhal number, drag coefficient, pumping power, and cylinder’s Nusselt number in proportion to increase in blockage ratio. Additionally, in their earlier publication [17], they found that onset of unsteady periodicity occurs for $Re\geq50$. Also, Tatsutani et al. [18] studied this problem for a tandem of heated square cylinder; and Valencia [19] conducted a numerical study on flow and heat transfer in channel with a tandem of rectangular cylinder for a range of the Reynolds number between 100 and 400 and four different cylinder separation distances. Findings showed that the flow oscillations occur at $Re>100$ when the Reynolds number is based on the channel height, and the heat transfer from side walls of the channel increases by a factor of 1.78 in comparison with the plane channel. In 2007, De and Dalal [20] carried out a study on a heated triangular cylinder in laminar channel flow for a range of the Reynolds number based on maximum inlet velocity between 80 and 200 and a range of blockage ratio between $1/12$ and $1/3$. Their results showed that the Strouhal number and RMS of lift coefficient increase significantly with blockage ratio and Reynolds number while overall Nusselt number on triangular cylinder remains almost unchanged for different blockage ratios. Srikanth et al. [21] studied this problem for a range of Reynolds numbers between 1 and 80 and fixed blockage ratio of 0.25. They observed that the average Nusselt number and wake length increase and the mean drag coefficient decrease with increasing the Reynolds number. Also, they found critical Reynolds numbers between 58 and 59. Moreover, Ali et al. [22] experimentally investigated this problem for two positions of the equilateral triangular cylinder, when the vertex of the triangle faces the flow and the flat surface faces the flow, for a range of blockage ratios and a wide range of Reynolds numbers for turbulent regime. Effects of proximity of the channel wall to the triangular cylinder on flow and heat transfer from the channel side for Reynolds number ranges of 100–450 was numerically investigated by Farhadi et al. [23]. Results revealed that as triangular cylinder approaches the wall, the vortex shedding is removed and subsequently the heat transfer rate decreases. Yoon et al. [10] parametrically investigated the flow over inclined square cylinders to analyze different shedding topologies exhibited by the flow and also critical Reynolds numbers as the cylinder inclination varies from a symmetric to an asymmetric alignment about the horizontal centerline. Also, Agrwal et al. [24] experimentally studied the wake characteristics of a cylinder at several various inclinations at $Re=520$. Bao et al. [25] numerically investigated the flow past an equilateral cylinder using a two-step Taylor characteristic-based Galerkin method at different angles ($\alpha$) of flow. Results revealed that the triangular cylinder at $\alpha=0$ (side facing flow) experiences a higher drag force than the cylinder at $\alpha=60$ (apex facing flow). Tu et al. [26] studied the flow induced forces and flow characteristics of a triangular cylinder with various incident angles (0–60) at a wide range of Reynolds numbers ($Re=50–160$). It is seen that the incident angle greatly alters pressure distribution around the triangular cylinder. Several studies on flows over the cylinder have been carried out to analyze the thermal behavior of the
flow [27,28]. Chatterjee and Mondal [29] numerically analyzed unsteady flow and heat transfer case over a bluff body for different values of Prandtl number (Pr = 0.71, 7 and 100). Their results showed that the increase in Reynolds number affects the distribution of isotherms behind the body which results in reducing the heat transfer.

From flow field characteristics view point, generally, flow around bluff bodies is influenced by three distinct regions: boundary layer (continues from stagnation point to the separation point), shear-layer (from separation point to the closure of the recirculation bubble), and wake (from end of recirculation zone to the downstream where it refers to the shear-layers merge). Features of these regions at different Reynolds numbers is the basis of categorizing flow into six regimes: no separation (creeping flow), a fixed pair of symmetric vortices, laminar vortex street, transition to turbulence in the wake, wake completely turbulent but laminar boundary layer, and turbulent wake and boundary layer. This paper is allocated to investigate the flow around bluff bodies in laminar boundary layer and wake where the most variation in flow characteristics (e.g. Strouhal number) happens.

Although several investigations set out to study the effects of bluff bodies on flow and heat transfer, various aspects of this problem have been remained unknown. This paper aims to investigate the effects of a triangular cylinder and six other different shapes of cylinders on heat transfer from side walls of the rectangular channel. It examines the drag coefficient on cylinder sides, skin-friction coefficient and Nusselt number on the channel wall, pumping factor, and Strouhal number for each model. Finally, efficiency of each cylinder shape in the enhancement of heat transfer is analyzed by the PI factor.

2. Numerical simulation

2.1. Assumptions

All models are simulated by commercial software COMSOL Multiphysics 5.2a under the assumptions of laminar, incompressible, and unsteady flow. Also, the flow is assumed to be two-dimensional to prevent extra computational cost. The working fluid, air (Pr=0.71), is assumed to be Newtonian, and the viscous dissipation is neglected. Maximum temperature difference between the inlet fluid and the wall of the channel is 2K, so the physical properties are assumed to be constant.

2.2. Governing equations

As aforementioned assumptions are applied, the dimensionless mass conservation, x and y components of momentum, and energy conservation equations are transformed as follows respectively.

\[
\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0
\]

\[
\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = -\frac{\partial P}{\partial x} + \frac{1}{Re} \left( \frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} \right)
\]

\[
\frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} = -\frac{\partial P}{\partial y} + \frac{1}{Re} \left( \frac{\partial v}{\partial x} + \frac{\partial v}{\partial y} \right)
\]

\[
\frac{\partial \theta}{\partial t} + u \frac{\partial \theta}{\partial x} + v \frac{\partial \theta}{\partial y} = \frac{1}{Re \cdot Pr} \left( \frac{\partial^2 \theta}{\partial x^2} + \frac{\partial^2 \theta}{\partial y^2} \right)
\]

\[u, v, x, y, t, \theta, P, Re, \text{ and } Pr\] are dimensionless \(x\) and \(y\) components of velocity, axial and transverse coordinates (Cartesian), time, temperature, pressure, Reynolds number, and Prandtl number are defined respectively as follows:

\[u = \frac{u^*}{U_{in}}, \quad v = \frac{v^*}{U_{in}}, \quad x = \frac{x^*}{H}, \quad y = \frac{y^*}{H},\]

\[t = \frac{t^* U_{in}}{L}, \quad \theta = \frac{T - T_{in}}{T_w - T_{in}}, \quad P = \frac{P^*}{\rho U_{in}^2}, \]

\[Re = \frac{\rho U_{in} b}{\mu}, \quad Pr = \frac{\mu C_p}{k},\]

where superscript * is related to dimensional variables, and subscripts in and \(W\) denote inlet and wall conditions. \(U_{in}, H, L, T, \rho, \mu, C_p, \text{ and } k\) are, respectively, the maximum of inlet velocity, channel height, channel length (L=10H), dimensional temperature, density, dynamic viscosity, specific heat at constant pressure, and thermal conductivity.

2.3. Boundary conditions

Inlet conditions are given as follows:
and $\theta = 0$. In COMSOL Multiphysics 5.2a; it is recommended to use a step function for ramping up the inlet velocity due to avoiding inconsistency between initial and inlet conditions. Velocity conditions on walls are defined as no-slip ($u = 0$ and $v = 0$) and thermal conditions on channel walls are $\partial \theta / \partial y = 0$ for $x < x_e$ and $x > x_e$, $\theta = 1$ for $x_e \leq x \leq x_e$, and on cylinder surface is $\partial \theta / \partial n = 0$ where $n$ is the normal direction to cylinder surface. Outlet conditions are $P = 0$, which is defined relative to atmosphere pressure, and $\partial \theta / \partial x = 0$.

### 2.4. Defined numbers

Efficiency of channel in enhancement of heat transfer with regard to pressure drop is denoted by Eq. (6).

$$PL = \frac{\overline{Nu}}{\overline{Nu}_0} \left( \frac{f}{f_0} \right)^{1/3}$$

where $\overline{Nu}$ and $f$ that are the Nusselt number and pumping factor, are presented in Eqs. (7 and 8).

$$\overline{Nu} = \sqrt{\left( \frac{\partial T}{\partial x^*} \right)^2 + \left( \frac{\partial T}{\partial y^*} \right)^2} \times H$$

$$f = \frac{2D_H \Delta P}{L}$$

where $\Delta P$ is the non-dimensional pressure difference between inlet and outlet and $D_H$ is the hydraulic diameter of the channel cross section defined as $D_H = \frac{4A_C}{P_C} \equiv 2H$, where $A_C$ and $P_C$ are area and wetted perimeter of cylinders cross section.

In Eq. (6), subscript 0 denotes the values of plain channel with no cylinder and the tild mark is the time average as follows:

$$\phi = \frac{1}{t_e - t_s} \int_{t_e}^{t_s} \phi \, dt$$

where $\phi$ can be any of the parameters, e.g. $Nu$, $f$, $C_f$ etc., and the over-bar is the space average as below:

$$\overline{\phi} = \frac{1}{x_e - x_s} \int_{x_e}^{x_s} \phi \, dt$$

Skin-friction coefficient is given as below:

$$C_f = \frac{2\tau_w}{\rho U_{in}^2}$$

where $\tau_w$ is the total shear stress on the wall and is defined as:

$$\tau_w = \mu \left( \frac{\partial u^*}{\partial y^*} + \frac{\partial v^*}{\partial x^*} \right)$$

Moreover, drag coefficient for cylinders is

$$C_D = \frac{2F_D}{\rho U_{in}^2 b}$$

where $F_D$ is the drag force per unit length. Strouhal number is defined as:

$$St = \frac{\omega b}{U_{in}}$$

where $\omega$ is the vortex shedding frequency (Hz).

### 2.5. Geometry

Geometry of the channel and cylinders is depicted in Fig. 1. As it shows for the first model, $x_e$, the end of the cylinder, is the beginning of the heated part of the wall. The fully developed flow enters from the left side with Eq. (5) and exits the right side. Moreover, the blockage ratio is defined as $\beta = b/H$.

### 2.6. Time stepping and grid independency

A combination of triangular and quadrilateral elements is used in internal region. Two layers of quadrilateral elements are applied at boundary layer, and the mesh is calibrated for fluid dynamics. The results of grid independency for equilateral triangular cylinder at $Re=150$ and $\beta=0.25$ and corresponding values for $Nu$ and $f$ are presented in Table 1. Eventually, grid number 3 is used due to acceptable accordance with the results of Srikanth et al. [21] and De and Dalal [20].
Computational domain is comprised of 297259 triangular elements and 6338 quadrilateral elements, where 3353 of them are in boundary layer. The maximum and minimum element sizes are 0.0635b and 0.0039b, respectively. Also, a dimensionless time step of 0.003 is considered. It should be noted that in order to neglect the early effects of the flow before \( t_s \), limits of the time integral in Eq. (9) are considered to be \( t_s \) and \( t_e \). As a result, \( t_s \) is the begging of the vortex shedding, and \( t_e \) is assumed to be long enough, about \( (5 \times L) / U_{in} \). Moreover, \( x_s \) and \( x_e \), limits of the space integral in Eq. (10), are 1.5 and 7.5 for \( Nu \) and 0 and 10 for \( C_f \).

3. Results and discussion

3.1. Validation

The present paper is validated by works of Srikanth et al. [21] and De and Dalal [20]. Values of drag coefficient and Strouhal number for equilateral triangular cylinder for \( \beta = 0.25 \) are presented in Table 2. The results show, for instance at \( Re = 150 \), 0.08% and 0.5% differences for drag coefficient and Strouhal number with the values of Srikanth et al. [21] and 1.2% and 2.2% differences with the values of De and Dalal [20], respectively. Therefore, the differences are considered acceptable and this simulation is considered to be valid.

3.2. Flow analyzing

First of all, effects of variation in blockage ratio and Reynolds number on flow over the equilateral triangular cylinder is investigated. Variation of drag coefficient with blockage ratio is presented in Fig. 2. The trend shows that drag coefficient increases with an increase in blockage ratio. The drag is the force exerted by the fluid on the body in the direction of the flow. This force consists of two components: friction drag and pressure drag. The friction drag is applied by the shear stress on the surface of the body while the pressure drag stems from the pressure difference between the fore and aft of the body. Since the drag coefficient \( (C_D) \) is independent of size of the obstacle and includes both pressure and friction drag, this rise with the blockage ratio can be interpreted by the growth of the wake region since the frictional component of the drag is constant for different sizes.

Fig. 3 shows this phenomenon clearly. These results are reported by De and Dalal [20] for triangular cylinder with \( 1/12 \leq \beta \leq 1/3 \) as well. In contrast, the growing of the drag coefficient with an increase in the Reynolds number is diminutive. Although this rise from an increase in Reynolds number reinforces the generation of the wake region, which augments the drag coefficient; it expands the growth of the boundary layer on the surface of the cylinder. Growth in thickness of the boundary layer reduces the velocity gradient perpendicular to the surface of the body and reduces the friction drag. Furthermore, damping effects of the wall proximity at \( \beta = 0.35 \) attenuates the generation of the wake. Davis et al. [30] reported this increase of drag coefficient with the Reynolds number for a square cylinder, and De and Dalal [20] reported it for a triangular cylinder as well.

Fig. 4 shows skin-friction coefficient as a function of the blockage ratio and Reynolds number. With an increase in the blockage ratio and approaching the cylinder to the channel wall, the velocity gradient increases in the region between the wall and the cylinder. This phenomenon is the major contributor in increasing the mean skin-friction coefficient with blockage ratio (Fig. 5). Moreover, it is observed that an increase in Reynolds number decreases the skin-friction coefficient. This means that the rise in velocity is dominant against the velocity gradient in Eq. (11).

One of the major characteristics of flow around bluff bodies is the Strouhal number which denotes the frequency of the vortex shedding upon inertia force. To put it simply, Strouhal number is a measurement of the possibility and strength of vortex shedding.

Before flow begins to fluctuate, a pair of fixed vortices first appears in the wake of the cylinder. When Reynolds number reaches to its critical value, these vortices, which by now have stretched and elongated, become unstable and the first periodic driving forces begin. The subsequent behavior of this vorticity strongly influences the flow development and the forces acting on the body. Particularly, these vortices have strong influence on mass and heat mixture. Vortex shedding frequency is equal to the period of the fluctuations of perpendicular velocity component. Variation of the Strouhal number with \( \beta \) and \( Re \) is presented in Fig. 6.
Table 1. Grid independency for equilateral triangular cylinder at Re=150 and β=0.25.

<table>
<thead>
<tr>
<th>Grid number</th>
<th>Total triangular elements</th>
<th>Total quadrilateral elements</th>
<th>Boundary elements</th>
<th>Nu</th>
<th>f</th>
</tr>
</thead>
<tbody>
<tr>
<td>G1</td>
<td>49097</td>
<td>3282</td>
<td>1731</td>
<td>6.3633</td>
<td>0.16229</td>
</tr>
<tr>
<td>G2</td>
<td>115311</td>
<td>6338</td>
<td>3309</td>
<td>6.4306</td>
<td>0.16772</td>
</tr>
<tr>
<td>G3</td>
<td>297259</td>
<td>6338</td>
<td>3353</td>
<td>6.5240</td>
<td>0.17495</td>
</tr>
</tbody>
</table>

Table 2. Validation by Srikanth et al. [21] and De and Dalal [20] for equilateral triangular cylinder for β=0.25.

<table>
<thead>
<tr>
<th>Source</th>
<th>CD</th>
<th>St</th>
</tr>
</thead>
<tbody>
<tr>
<td>Present paper</td>
<td>1.6503</td>
<td>0.1900</td>
</tr>
<tr>
<td>Srikanth et al. [21]</td>
<td>1.6357</td>
<td>0.1919</td>
</tr>
<tr>
<td>De and Dalal [20]</td>
<td>1.64</td>
<td>0.195</td>
</tr>
<tr>
<td>Present paper</td>
<td>1.6817</td>
<td>0.2000</td>
</tr>
<tr>
<td>Srikanth et al. [21]</td>
<td>1.6708</td>
<td>0.2004</td>
</tr>
<tr>
<td>De and Dalal [20]</td>
<td>1.68</td>
<td>0.205</td>
</tr>
<tr>
<td>Present paper</td>
<td>1.9364</td>
<td>0.2200</td>
</tr>
<tr>
<td>Srikanth et al. [21]</td>
<td>1.9349</td>
<td>0.2212</td>
</tr>
<tr>
<td>De and Dalal [20]</td>
<td>1.96</td>
<td>0.225</td>
</tr>
</tbody>
</table>

Fig. 1. Geometry of the problem.

Fig. 2. Variation of the drag coefficient with the Reynolds number at β=0.35 and blockage ratio at Re=150 for triangular cylinder.

It reveals that at high blockage ratios effects of side walls are noteworthy, which make the frequency of the vortex shedding shift to higher values. This is in agreement with the results of De and Dalal [20] for the triangular cylinder at 1/12≤β≤1/3, and Patil et al. [31] for the square cylinder at 0.2≤β≤0.5. Also, an increase in Reynolds number for constant blockage ratio increases the Strouhal number, but not as much as the blockage ratio. An increase in Strouhal number with Reynolds number is reported by Srikanth et al. [21] and De and Dalal [20] for the triangular cylinder, Sharma and Eswaran [16] for the square cylinder and Norberg [32] for the circular cylinder.
Fig. 7 demonstrates the variation of the pumping factor with the blockage ratio and Reynolds number. Pumping factor is a measurement of all dissipations in flow field, including wall friction and drag force. This coefficient, particularly, is used in calculation of the Performance Index (PI) factor. As expected, with an increase in the blockage ratio, the pumping factor increases significantly as a result of rise in both drag and skin-friction coefficient; but with an increase in Reynolds number, pumping factor decreases slightly. This means that the decrease in the skin-friction dominates the increase of drag coefficient. After investigating the effects of variation in Reynolds number and blockage ratio on flow characteristics, at this point, attention is turned toward variation in the shape of the cylinder. This part of the investigation is conducted to enhance the heat transfer efficiency (PI factor). As in Eq. (6), the PI factor is composed of Nusselt number and pumping factor. Nusselt number will be discussed in subsection 3.3. Effects of modifying the shape of the cylinder on pumping factor will be discussed here. Additionally, to give more information and better illustration of flow around different cylinders, other coefficients are presented as well. In order to compare the impacts of different shapes of the cylinder, Reynolds number and blockage ratio are, respectively, assumed to be 180 and 0.35. At these values, fluctuation of the flow has the highest effect on the walls of the channel while damping effect of the walls on generation of the vortex shedding is the lowest. Comparing Figs. 8, 9, and 11 confirms that fore and aft pressure difference, also, is responsible for an increase in skin-friction coefficient.
As the pressure difference increases, flow becomes more turbulent and velocity gradient rises near the wall. This leads to higher shear stress and skin-friction coefficient. Furthermore, the pumping factor, which can be explained as total effects of the drag force and shear stress, follows the same pattern in different shapes.

Figs. 11 and 12 present values of Strouhal number and streamlines for different shapes of the cylinder, respectively. Streamlines represent vortices that have a direct effect on the Stockholm number. Generally, Strouhal number depends on Reynolds number, the shape of the body, and the blockage ratio. Continuous shapes have no fixed disseverment point. Therefore, it is more dependent on the Reynolds number; but in discontinuous shapes, the type and position of the vertices are important. For models 2 and 7, which have the highest values of the $C_D$, $C_f$, and $f$, it is observed that the Strouhal number has the minimum values. On the other hand, it has the maximum value in model 4. Similarities in structure and geometry of the vortex shedding from different shapes drew attention of the scientists to the relationship between Strouhal number and size of the wake; Ahlborn et al. [33] and Balachandar et al. [34], for instance, made some effort on this aspect.

3.3. Heat transfer analyzing

Variation of the Nusselt number, which is a measurement of the heat transfer from side walls of the channel, versus Reynolds number and blockage ratio for equilateral triangular cylinder is presented in Fig. 13. As this figure demonstrates, an increase in Reynolds number augments vortex shedding and induces turbulent effects. Subsequently, this fluctuation improves mixing of the cold and hot fluid. In contrast, with an increase in blockage ratio, Nusselt number reaches to an optimum value at $\beta=0.35$. By more increase in blockage ratio, Nusselt number, as a result of damping effect of the walls on generation of the vortex shedding, declines and by then plummets down at $\beta=0.55$. However, at low blockage ratios ($\beta=0.15$), it is observed that Nusselt number is higher. This is caused by the high inlet velocity. As mentioned earlier, at this blockage ratio the effect of the fluctuation of flow on side walls is trivial. More precisely, Fig. 14 clarifies the distribution of the Nusselt number for different blockage ratios. The impact of vortex shedding on heat transfer enhancement and decrease in heat transfer due to destruction of the vortex shedding is clearly shown in this figure and Fig. 15.
Fig. 11. Values of the Strouhal number for different shapes of the cylinder at Re=180 and β=0.35.

Fig. 13. Variation of Nusselt number with blockage ratio at Re=150 and Reynolds number at β=0.35 for triangular cylinder.

Fig. 14. Distribution of the Nusselt number for triangular cylinder for different blockage ratios at Re=150.

Fig. 16 presents values of the Nusselt number for different shapes of the built-in cylinder at Re=180 and β=0.35. This figure reveals that model number seven and two have the highest values of the Nusselt number, respectively. By comparing Fig. 16 with Figs. 8, 9, and 10, it can be inferred that, generally, for models with stronger wake region, Nusselt number is higher. The reason is that by increasing the pressure difference between fore and aft of the cylinder, more fluid with higher velocity flows toward back of the cylinder. This phenomenon makes the flow more turbulent, which induces higher values of the Nusselt number. Perturbation of the thermal boundary layer for each cylinder is depicted in Fig. 17.

3.4. Thermal efficiency

The PI factor defines thermal efficiency of a channel in heat transfer enhancement with regard to the pumping factor. Fig. 18 shows PI factor as a function of blockage ratio and Reynolds number for the equilateral triangular cylinder (model one). As can be seen, with an increase in the Reynolds number the PI factor slightly decreases. Moreover, for different blockage ratios, the PI factor has an optimum range between β=0.35 and β=0.45. Fig. 19 presents the values of the PI factor for different shapes of the cylinder at Re=180 and β=0.35. As this figure shows, the best cylinder shape from the thermal efficiency viewpoint is model seven with PI=0.9736.
Fig. 15. Isothermal contours for different blockage ratios of the equilateral triangular cylinder at Re=150.

Fig. 16. Values of the Nusselt number for different shapes of the cylinder at Re=180 and β=0.35.

Fig. 17. Isothermal contours for different shapes of the cylinder at Re=180 and B=0.35.
4. Conclusions

The present study is conducted to investigate 2-D laminar air flow and heat transfer characteristics of a channel with a built-in cylinder. Variation of the cylinder’s drag coefficient, Strouhal number, skin-friction factor, pumping factor, Nusselt number from side walls of the channel, and PI factor for 120≤Re≤180 and 0.15≤β≤0.55 is studied for the equilateral triangular cylinder. Results show that for the constant blockage ratio of 0.35, the drag coefficient, Nusselt number, and Strouhal number increase, but the skin-friction coefficient, pumping factor, and PI factor decrease with an increase in Reynolds number.

Also, with increase in blockage ratio at constant Reynolds number, Re=150, the drag coefficient, skin-friction coefficient, Strouhal number, and pumping factor increase, but the Nusselt number decreases and the PI factor shows an optimum range for 0.35≤β≤0.45. Moreover, it is seen that variation in the blockage ratio has more significant effects on flow characteristics. For β>0.45 fluctuation of flow is destroyed by damping effects of the side walls. In the second orientation, variation in the shape of the built-in cylinders is investigated for seven different types of geometry. Findings prove that values of the drag coefficient, skin-friction coefficient, pumping factor, and Nusselt number are higher for the second and seventh models. Furthermore, results show a direct correlation between the drag coefficient, skin-friction coefficient, pumping factor, and Nusselt number. Finally, the maximum accessible PI factor of 0.9736 is obtained for the seventh model.

References


