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Effects of heat generation and thermal radiation on steady MHD flow near a stagnation point on a linear stretching sheet in porous medium and presence of variable thermal conductivity and mass transfer

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Article info:	Abstract
Received: 17/01/2014	The present paper was aimed to study the effects of variable thermal conductivity
Accepted: 12/06/2014	and heat generation on the flow of a viscous incompressible electrically conducting
Online: 03/03/2015	fluid in the presence of a uniform transverse magnetic field, thermal radiation,
	porous medium, mass transfer, and variable free stream near a stagnation point on a
Keywords:	non-conducting stretching sheet. Equations of continuity, momentum, energy, and
Boundary layer,	mass were transformed into ordinary differential equations and solved numerically
Steady,	using shooting method. Velocity, temperature, and concentration distributions were
MHD,	numerically discussed and presented in the graphs. Skin-friction coefficient, the
Stagnation point,	Nusselt number, and Sherwood number on the sheet were derived and discussed
Radiation,	numerically. Their numerical values for various values of physical parameters were
Mass transfer,	presented in the tables. It was found that temperature increased with increasing
Porous medium,	radiation parameter, R, and concentration decreased with increasing the Schmidt
Heat generation.	number, Sc. The numerical predications were compared with the existing
	information in the literature and a good agreement was obtained.

1. Introduction

In fluid dynamics, effects of external magnetic field on magneto hydrodynamic (MHD) flow over a stretching sheet are very important because of applications in many engineering problems, such as glass manufacturing, geophysics, paper production, and crude oil purification. The flow related to the stretching of a flat surface was first investigated by Crane [1]. Pavlov [2] studied the effect of external magnetic field on the MHD flow over a

*Corresponding author Email address: ibrahimsvu@gmail.com stretching sheet. Andersson [3] discussed the MHD flow of viscous fluid on a stretching sheet. Mukhopadhyay et al. [4] presented the MHD flow and heat transfer over a stretching sheet with variable fluid viscosity. Bhattacharyya and Layek [5] showed the behavior of solute distribution in the MHD boundary layer flow past a stretching sheet. Furthermore, many vital properties of MHD flow over stretching sheet have been explored in articles [6-8] in the related literature.

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The field of boundary layer flow problem over a stretching sheet has many industrial applications, such as in polymer sheet, filament extrusion from a dye, long thread between feed roll or wind-up roll, glass fiber and paper production, drawing of plastic films, and liquid films in condensation process. Due to the high applicability of this problem in such industrial phenomena, it has attracted the attentions of many researchers. Sakiadis [9] was the first who studied boundary layer flow over a stretching surface moving at constant velocity in an ambient fluid. He employed a similarity transformation and obtained a numerical solution for the problem. Erickson et al. [10] extended the work of Sakiadis [9] to account for mass transfer on the stretching surface. Tsou et al. [11] presented a combined analytical and experimental study on the flow and temperature field in the boundary layer on a continuous moving surface. Noghrehabadi et al. [12] studied the effect of partial slip boundary conditions on the flow and heat transfer of nanofluids past stretching sheet prescribed constant wall temperature. Noghrehabadi et al. [13] analyzed the flow and heat transfer of nanofluid over stretching sheet while taking account particle slip and thermal into convective boundary conditions.

The stagnation point flows are classic problems in the field of fluid dynamics and have been investigated by many researches. These flows can be viscous or in viscid, steady or unsteady, two-dimensional or three-dimensional, normal or oblique, and forward or reverse. The steady flow in the neighborhood of a stagnation point was first studied by Hiemenz [14], who used a similarity transformation to reduce the Navier-Stokes equations to nonlinear ordinary differential equations. This problem was extended by Homann [15] to the case of axisymmetric stagnation point flow. Stagnation point flows have been discussed by Pai [16], Schlichting [17], Bansal [18], Chiam [19], etc. Mahapatra and Gupta [20] and Nazar et al. [21] have investigated the heat transfer in the steady two-dimensional stagnation point flow of a viscous fluid by taking different aspects into account.

Kay [22] proposed that thermal conductivity of liquids with low Prandtl number varied linearly with temperature in the range of 0 to 400° F. Arunachalam and Rajappa [23] considered forced convection in liquid metals (i.e. fluid with low Prandtl number) with variable thermal conductivity and capacity in the potential flow and derived an explicit closed form of analytical solution. Fluid flow and heat transfer characteristics on stretching sheet with variable temperature conditions were investigated by Grubka and Bobba [24]. Chaim [25] studied heat transfer in the fluid flow of low Prandtl number with variable thermal conductivity induced as a result of stretching sheet and compared the numerical results with the perturbation solution.

Effect of thermal radiation on flow and heat transfer processes is of major importance in the design of many advanced energy conversion systems operating at high temperature. Thermal radiation within such systems occurs because of the emission by the hot walls and working fluid. Pop et al. [26] discussed the flow over stretching sheet near a stagnation point while considering thermal radiation effect. The effect of radiation on heat transfer problems was studied by Hossain and Takhar [27]. Pal [28] investigated heat and mass transfer in stagnation point flow towards a stretching surface in the presence of buoyancy force and thermal radiation. Vyas and Srivastava [29] presented a numerical study for the steady twodimensional radiative MHD boundary laver. with a reference to the flow of an incompressible, viscous. and electrically conducting fluid caused by a non-isothermal linearly stretching sheet placed at the bottom of a fluid saturated porous medium.

The study of heat generation or absorption in moving fluids is important in the problems dealing with chemical reactions and those concerned with dissociating fluids. Possible heat generation effects may alter temperature distribution, which may influence particle deposition and distribution rate; hence, the particle deposition and distribution rate in the conductor wafers. The steady hydromagnetic laminar stagnation point flow of an incompressible viscous fluid impinging on a permeable stretching surface with heat generation or absorption was analyzed by Attia [30]. Sharma and Singh [31] investigated the effects of variable thermal conductivity and heat source/sink on flow near a stagnation point on a non- conducting stretching sheet. Effects of variable thermal conductivity and heat source/sink two-dimensional on steady radiative MHD boundary layer flow of a incompressible, and viscous. electrically conducting fluid in the presence of variable free steam near a stagnation point on a nonconducting stretching sheet was investigated by Al-Sudais [32]. Noghrehabadi et al. [33] analyzed the boundary layer heat transfer and entropy generation of a nanofluid over an isothermal linearly stretching sheet with heat generation/absorption.

The objective of this study was to extend the work by Al-Sudais [32], considering the mass transfer. The governing equations were transformed using similarity transformation and the resultant dimensionless equations were solved numerically using the Runge-Kutta fourth order method by shooting technique. The effects of various governing parameters on the velocity, temperature, concentration, skinfriction coefficient, the Nusselt number, and Sherwood number are shown in figures and tables and analyzed in detail. To the best knowledge of the present authors, this problem has not been studied before.

2. Formulating the problem



Fig. 1. Sketch of the physical model.

Consider a steady two-dimensional flow of viscous incompressible electrically conducting fluid with variable thermal conductivity in the vicinity of a stagnation point on a nonconducting stretching sheet in the presence of transverse magnetic field and volumetric rate of heat generation. The stretching sheet has uniform temperature, $T_{\rm w}$, and linear velocity, $u_w(x)$. It is assumed that external field is zero and the electric field owing to the polarization of charges and Hall effect is neglected. Stretching sheet is placed in the plane v = 0and x-axis is taken along the sheet, as shown in Fig. 1. The fluid occupies the upper half plane i.e. v > 0. The governing equations of continuity. momentum, energy, and concentration under the influence of externally imposed transverse magnetic field (Bansal [18]) with variable thermal conductivity in the boundary layer are:

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \tag{1}$$

$$u\frac{\partial u}{\partial x} + v\frac{\partial u}{\partial y} = -\frac{1}{\rho}\frac{\partial p}{\partial x} + v\frac{\partial u}{\partial y^2} - \frac{\partial D_0}{\rho}u - \frac{v}{K^*}u$$
(2)

$$\rho c_{p} \left(u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} \right) = \frac{\partial}{\partial y} \left(k^{*} \frac{\partial T}{\partial y} \right) - \frac{\partial q_{r}}{\partial y} + Q^{*} \left(T - T_{\infty} \right)$$
(3)

$$u\frac{\partial C}{\partial x} + v\frac{\partial C}{\partial y} = D\frac{\partial^2 C}{\partial y^2}$$
(4)

where x and y represent the coordinate axes along the continuous stretching surface in the direction of motion and normal to it, respectively; u and v are the velocity components along the x and y axes, respectively; p is the pressure of the fluid; v is the kinematic viscosity; σ is electrical conductivity; B_0 is the magnetic field intensity; ρ is the fluid density; K^* is the permeability of the porous medium; c_n is the specific heat at constant pressure; q_r is the radiation heat flux; T is the fluid temperature; T_{∞} is the fluid free steam temperature; T_w is the fluid temperature of stretching sheet; C is the fluid concentration; C_{∞} is the fluid free stream concentration; C_w is the fluid concentration of stretching sheet; k^* is the variable thermal conductivity; Q^* is the volumetric rate of heat generation; and D is the molecular diffusivity of the species concentration.

The second derivatives of u and T with respect to x are eliminated on the basis of magnitude analysis considering that Reynolds number is high. Hence, the Navier-Stokes equation is modified into Prandtl's boundary layer equation.

In the free stream u = U(x) = bx, Eq. (2) is reduced to:

$$U\frac{dU}{dx} = -\frac{1}{\rho}\frac{\partial p}{\partial x} - \frac{\sigma B_0^2}{\rho}U$$
(5)

By eliminating $\frac{\partial p}{\partial x}$ between Eqs. (2 and 5), the

following is obtained:

$$u\frac{\partial u}{\partial x} + v\frac{\partial u}{\partial y} = U\frac{dU}{dx} + v\frac{\partial^2 u}{\partial y^2} - \frac{\sigma B_0^2}{\rho}(u-U) - \frac{v}{K^*}u$$
(6)

The boundary conditions for the present problem are:

 $u = u_w(x) = cx$, v = 0, $T = T_w$, $C = C_w$ at y = 0,

$$u = U(x) = bx, \quad T = T_{\infty}, \qquad C = C_{\infty} \qquad as$$

$$y \to \infty. \qquad (7)$$

Using the Rosseland approximation for radiation (Brewster [34]), the radiative heat flux q_r could be expressed by:

$$q_r = -\frac{4\sigma^*}{3k_0}\frac{\partial T^4}{\partial y} \tag{8}$$

where σ^* represents the Stefan-Boltzman constant and k_0 is the Rosseland mean absorption coefficient. By assuming that the 136

temperature difference within the flow is such that T^4 may be expanded in a Taylor series about T_{∞} and neglecting higher orders, the following is obtained:

$$T^4 \cong 4T_\infty^3 T - 3T_\infty^4 \tag{9}$$

Following Arunachalam and Rajappa [23] and Chaim [25], thermal conductivity k^* is taken with the form as given below:

$$k^* = k \left(1 + \varepsilon \theta \right) \tag{10}$$

The continuity Eq. (1) is satisfied by introducing the stream function $\psi(x, y)$ such that:

$$u = \frac{\partial \psi}{\partial y}$$
 and $v = -\frac{\partial \psi}{\partial x}$

The following non-dimensional variables are introduced:

$$\psi(x, y) = (cv)^{\frac{1}{2}} xf(\eta), \qquad \eta = \left(\frac{c}{v}\right)^{\frac{1}{2}} y,$$

$$\theta(\eta) = \frac{T - T_{\infty}}{T_{w} - T_{\infty}}, \quad \phi(\eta) = \frac{C - C_{\infty}}{C_{w} - C_{\infty}}, \quad \lambda = \frac{b}{c},$$

$$K = \frac{v}{K^{*}c}, \qquad M = \frac{\sigma B_{0}^{2}}{\rho c}, \qquad R = \frac{16\sigma^{*}T_{\infty}^{3}}{3k_{0}k},$$

$$\Pr = \frac{\mu c_{p}}{k}, \qquad Q = \frac{Q^{*}}{\rho c_{n}c}, \qquad Sc = \frac{v}{D}.$$
 (11)

Using Eqs. (8-11) in Eqs. (6, 3 and 4), the following ordinary differential equations can be obtained:

$$f''' + ff'' - f'^{2} - M(f' - \lambda) - Kf' + \lambda^{2} = 0,$$
(12)

$$(1+R+\varepsilon\theta)\theta''+\varepsilon\theta'^2+\Pr f\theta'+\Pr Q\theta=0$$
 (13)

$$\phi'' + Scf \,\phi' = 0 \tag{14}$$

where the primes denote the differentiation with respect to η , λ is the ratio of free stream velocity parameter to stretching sheet parameter, *b* is the free stream velocity parameter, *c* is the stretching sheet parameter,

M is the magnetic parameter, K is the permeability parameter, Pr is the Prandtl number, R is the thermal radiation parameter, Е is perturbation parameter, Q is the heat generation parameter, and Sc is the Schmidt number.

The corresponding boundary conditions are reduced to:

$$f(0) = 0, \quad f'(0) = 1, \quad \theta(0) = 1, \quad \phi(0) = 1 f'(\infty) = \lambda, \quad \theta(\infty) = 0, \quad \phi(\infty) = 0$$
(15)

3. Skin-friction coefficient, the Nusselt number and Sherwood number

In practical applications, three quantities of physical interest are to be determined, such as surface shear stress, rate of heat transfer, and rate of mass transfer on the surface. They may be obtained in terms of the skin friction coefficient:

$$C_f = \frac{\tau_w}{\rho c \sqrt{cv}} = x f''(0) \tag{16}$$

The local Nusselt number:

$$Nu = \left(\frac{v}{c}\right)^{\frac{1}{2}} \frac{q_w}{k^* (T_w - T_\infty)} = -\theta'(0) \tag{17}$$

and the local Sherwood number:

$$Sh = \left(\frac{v}{c}\right)^{\frac{1}{2}} \frac{m_w}{D(C_w - C_\infty)} = -\phi'(0) \tag{18}$$

where $\tau_w = \mu \left(\frac{\partial u}{\partial v} + \frac{\partial v}{\partial x} \right)_{u=0}$ is the shear-stress

along the sheet

$$q_w = -k^* \left(\frac{\partial T}{\partial y}\right)_{y=0}$$
 is the surface heat transfer

rate, and $m_w = -D\left(\frac{\partial C}{\partial y}\right)_{y=0}$ is the surface mass

transfer rate.

4. Method of solution

The governing boundary layer, thermal and concentration boundary layer Eqs. (12-14) with the boundary conditions (15) are solved using Runge-Kutta fourth order technique along with shooting method (Conte and Boor [35]). First of all, higher order non-linear differential Eqs. (12-14) are converted into simultaneous linear differential equations of order first and further transformed into initial value problem by the shooting technique. Once the problem is reduced to the initial value problem, it is solved using Runge-Kutta fourth order technique (Jain [36], Jain et al. [37], Krishnamurthy and Sen [38]).

5. Results and discussion

system of non-linear ordinary differential Eqs. (12-14) is solved numerically using shooting method for different values of magnetic field parameter, M, permeability of the porous medium, K, ratio of free stream velocity parameter to stretching sheet parameter, λ , thermal radiation parameter, R, the Prandtl number, Pr, heat generation parameter, Q, perturbation parameter, ε , and the Schmidt number. Sc.

In order to assess the accuracy of the numerical method, results for f''(0) in the absence of magnetic field parameter (M = 0) are compared with those of Pop et al. [26], Mahapatra and Gupta [20], and Al-Sudais [32]. The first used Runge-Kutta fourth order method and shooting technique, while the second applied finite difference technique and Thomas algorithm; the last one used Runge-Kutta fourth order method along with shooting technique. The result of the comparison found a good agreement among them. These comparisons are shown in Table 1. It is seen from table 2 that the numerical values of $-\theta'(0)$ in the present paper, when M = K = $R = Q = Sc = \varepsilon = 0$ and Pr = 0.05, are in agreement with those obtained by Pop et al. [26], Mahapatra and Gupta [20], and Al-sudais [32].

To analyze the results, numerical computations are carried out for variations in the governing parameters such as magnetic field parameter, M, permeability of the porous medium, K, ratio of free stream velocity parameter to stretching thermal λ, radiation sheet parameter, parameter, R, the Prandtl number, Pr, heat 137

generation parameter, Q, perturbation parameter, ε , and the Schmidt number, Sc.

In the present study, the following default parameter values are adopted for computations: M = 0.1, K = 0.1, Pr = 0.71, R = 1.0, Q = 0.1, $\lambda = 0.1, \varepsilon = 0.1, Sc = 0.22.$

All graphs therefore correspond to these values unless specifically indicated in the appropriate graph.

Figure 2 represents the importance of magnetic field for the velocity profiles. The presence of transverse magnetic field parameter M is set in Lorentz force, which results in retarding force on the velocity filed. Therefore, as magnetic field parameter increases, so does the retarding force and hence the velocity profiles decreases, as shown in Figure 2. Figures 3 and 4 display the temperature and concentration profiles with magnetic field parameter, respectively. From these figures, it can be observed that both temperature and concentration profiles increase as magnetic field parameter increases.

The effect of the permeability of porous medium parameter, K, on velocity, temperature, and concentration profiles is shown in Figs. 5-7, respectively. It can be observed that velocity is reduced as the permeability of porous medium, K, increases, while temperature and concentration enhance as the permeability of porous medium, K, increases, while temperature and concentration enhance as the permeability of porous medium, K, increases, while temperature and concentration enhance as the permeability of porous medium, K, increases, which implies that the resistance of the medium is decreasing due to the increased restriction resulting from decreasing porosity of the porous medium.

Figure 8 illustrates the dimensionless temperature profiles for different values of the Prandtl number Pr. It is observed that an increase in the Prandtl number results in the decreased thickness of thermal boundary layer and in general lower average temperature within the boundary layer. The reason is that smaller values of the Prandtl number are equivalent to increasing the thermal conductivities; therefore, heat is able to diffuse away from the heated plate more rapidly than for higher values of Pr; in the case of smaller Prandtl number, as the boundary layer is thicker, the rate of transfer is reduced.

Figure 9 predicts the influence of the radiation parameter, R, on temperature field. The

radiation parameter, R, defines the relative contribution of conduction heat transfer to thermal radiation transfer. It is obvious that an increase in the radiation parameter results in increasing temperature within the boundary layer.

Figure 10 shows the influence of the heat generation parameter, Q, on temperature profiles within the thermal boundary layer. From Figure 10, it is observed that the temperature increases with an increase in the heat generation parameter, Q.

Figure 11 represents the temperature profiles for some values of the perturbation parameter, ε , and for fixed values of all others. Figure 11 represents that, with the increase in the value of ε , temperature profiles increase the thermal conductivity constant, leading to lower approximation of the temperature profile.

For different values of the Schmidt number, *Sc*, the concentration profile is plotted in Fig. 12. The Schmidt number, *Sc*, embodies the ratio of the momentum diffusivity to the mass (species) diffusivity. It physically relates the relative thickness of the hydrodynamic boundary layer and mass transfer (concentration) boundary layer. As the Schmidt number, *Sc*, increases, the concentration decreases, which causes the concentration buoyancy effects to decrease and yield a reduction in the fluid velocity. The reduction in the concentration profiles is accompanied by simultaneous reductions in the concentration boundary layers, which is evident in Fig. 12.

Figure 13 depicts the ratio of free steam velocity parameter to stretching sheet parameter, λ in velocity profiles. It is clear that the velocity profiles increase with an increase in the values of parameter λ . Figures 14 and 15 show the temperature and concentration profiles for different values of the ratio of free steam velocity parameter to stretching sheet parameter, λ . It is observed in Figs. 14 and 15 that fluid temperature and concentration decreases due to increased λ .

Effects of various governing parameters on the skin-friction coefficient, C_f , the Nusselt number, Nu, and the Sherwood number, Sh, are

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shown in Tables 3 and 4. It can be noticed that, as magnetic parameter M or permeability parameter K increase, the skin-friction coefficient increases and both Nusselt number and Sherwood number decrease. As λ increases, skin-friction coefficient is reduced, while the Nusselt number and Sherwood number increase. The Nusselt number increases



Fig. 2. Velocity Profiles for different values of M.



Fig. 4. Concentration profiles for different values of *M*.

as the Prandlt number increases, while Nusselt number is reduced as thermal radiation parameter, R, heat generation parameter, Q, or perturb bation parameter, ε increases. It is seen that the Sherwood number increases as an increase in the Schmidt number, Sc.



Fig. 3. Temperature profiles for different values of *M*.



Fig. 5. Velocity profiles for different values of K.



Fig. 6. Temperature profiles for different values of *K*.



Fig. 8. Temperature profiles for different values of *Pr*.



Fig. 10. Temperature profiles for different values of *Q*.



Fig. 7. Concentration profiles for different values of *K*.



Fig. 9. Temperature profiles for different values of *R*.



Fig. 11. Temperature profiles for different values of \mathcal{E}_{\perp}

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Fig. 12. Concentration profiles for different values of Sc.



Fig. 14. Temperature profiles for different values of λ



Fig. 13. Velocity profiles for different values of λ



Fig. 15. Concentration profiles for different values of λ .

λ	f''(0)	<i>f</i> "(0)				
	Pop et al. [26]	Mahapatra and Gupta [20]	Al-sudais [32]	Present paper		
0.1	-0.9694	-0.9694	-0.969705	-0.969385		
0.2	-0.9181	-0.9181	-0.918349	-0.9181065		
0.5	-0.6673	-0.6673	-0.6674611	-0.667261		
2.0	2.0174	2.0175	2.01728138	2.0174904		

Table 1. Comparison of skin-friction coefficient f''(0) for different values of λ and M = 0.0.

Table 2. Comparison of the Nusselt number $-\theta'(0)$ for different values of λ when $M = Q = R = \varepsilon = 0.0, Pr = 0.05$.

2	- heta'(0)	- heta'(0)				
λ	Pop et al. [26]	Mahapatra and Gupta	Al-sudais [32]	Present paper		
		[20]				
0.1	0.081	0.081	0.080547	0.081241		
0.5	0.135	0.136	0.135358	0.135575		
2.0	0.241	0.241	0.241025	0.241029		

n 1.0, g	0.1,0 0.1,00 0.22.				
М	Κ	λ	C_{f}	Nu	Sh
0.1	0.1	0.1	-1.0602	0.268904	0.281977
0.3	0.1	0.1	-1.13321	0.262853	0.279277
0.5	0.1	0.1	-1.20198	0.257454	0.276908
0.1	0.3	0.1	-1.15376	0.257789	0.276929
0.1	0.5	0.1	-1.2398	0.248276	0.272698
0.1	0.1	0.3	-0.934202	0.304593	0.299526
0.1	0.1	0.5	-0.747837	0.344163	0.320372

Table 3. Numerical values of the skin-friction coefficient, Nusselt number and Sherwood number for Pr = 0.71, R = 1.0, Q = 0.1, $\mathcal{E} = 0.1$, Sc = 0.22.

Table 4. Numerical values of the skin-friction coefficient, Nusselt n	sumber and Sherwood number for $M = 0.1$,
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Pr	R	Q	Е	Sc	C_{f}	Nu	Sh
0.71	1.0	0.1	0.1	0.22	-1.0602	0.268904	0.281977
1.0	1.0	0.1	0.1	0.22	-1.0602	0.306422	0.281977
2.0	1.0	0.1	0.1	0.22	-1.0602	0.45044	0.281977
0.71	2.0	0.1	0.1	0.22	-1.0602	0.241735	0.281977
0.71	3.0	0.1	0.1	0.22	-1.0602	0.229604	0.281977
0.71	1.0	0.3	0.1	0.22	-1.0602	0.147114	0.281977
0.71	1.0	0.5	0.1	0.22	-1.0602	0.0723633	0.281977
0.71	1.0	0.1	0.3	0.22	-1.0602	0.236927	0.281977
0.71	1.0	0.1	0.5	0.22	-1.0602	0.20495	0.281977
0.71	1.0	0.1	0.1	0.6	-1.0602	0.268904	0.434922
0.71	1.0	0.1	0.1	0.94	-1.0602	0.268904	0.566934

6. Conclusions

In the present investigation, the effect of mass transfer on MHD mixed convection of steady fluid flow along a stretching sheet with variable thermal conductivity was studied in a porous medium with heat generation and thermal radiation. The governing boundary layer equations were transformed into a nondimensional form and the resulting nonlinear system of partial differential equations was reduced to local non-similarity boundary layer equations, which were solved numerically using Runge-Kutta fourth order technique along with shooting method. It can be drawn from the present results that, when radiation parameter increased, the heat transfer rate at the sheet decreased. It is seen that the Sherwood number increased as an increase in the Schmidt number. Also, the boundary layer flows were greatly influenced by the Prandtl number; as the Prandtl number increased, the sheet temperature gradients also increased. However, the temperature profiles decreased when the Prandtl number increased. Fluid velocity profiles decreased, whereas temperature and concentration profiles increased with an increase in magnetic field parameter.

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